

Lab 9 Shor's algorithm - using quantum period finding

Exercise 1

Get familiar with using period finding for factoring (e.g. see section H <http://www.lasp.cornell.edu/mermin/qcomp/chap3.pdf>)

Exercise 2

Use [period finding function](#) from last exercise to break RSA algorithm using simpler version (works with messages coprime with N)

Useful definitions:

b - encrypted message

G_N (i.e. group modulo N) - the set of all positive integers less than N (including 1) that have no factors in common with N.

d is the inverse modulo of *c* in G_N if $d*c=1 \pmod{N}$

The simpler version of RSA breaking algorithm:

1. Find *r* - period $b^x \pmod{N}$
2. Calculate *d'* - inverse modulo of *c* in G_r ,
3. Calculate decrypted message $a=b^{d'} \pmod{N}$

Note: you'll need auxiliary functions:

1. Euclidean algorithm for greatest common divisor (you can use [C# implementation](#))
2. Finding inverse modulo (you can use a loop with trying all possibilities or implement extended Euclidian algorithm)
3. Fast calculation of power using exponentiation by squaring (you can use [C# implementation](#))